



Mark Scheme (Results)

January 2023

Pearson Edexcel International Advanced Level In Mechanics M3 (WME03) Paper 01

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General Marking Guidance

- All candidates must receive the same treatment. Examiners must mark the first candidate in exactly the same way as they mark the last.
- Mark schemes should be applied positively. Candidates must be rewarded for what they have shown they can do rather than penalised for omissions.
- Examiners should mark according to the mark scheme not according to their perception of where the grade boundaries may lie.
- There is no ceiling on achievement. All marks on the mark scheme should be used appropriately.
- All the marks on the mark scheme are designed to be awarded. Examiners should always award full marks if deserved, i.e. if the answer matches the mark scheme. Examiners should also be prepared to award zero marks if the candidate's response is not worthy of credit according to the mark scheme.
- Where some judgement is required, mark schemes will provide the principles by which marks will be awarded and exemplification may be limited.
- When examiners are in doubt regarding the application of the mark scheme to a candidate's response, the team leader must be consulted.
- Crossed out work should be marked UNLESS the candidate has replaced it with an alternative response.

PEARSON EDEXCEL IAL MATHEMATICS

General Instructions for Marking

- 1. The total number of marks for this paper is 75.
- 2. The Edexcel Mathematics mark schemes use the following types of marks:

<u>'M' marks</u>

These are marks given for a correct method or an attempt at a correct method. In Mechanics they are usually awarded for the application of some mechanical principle to produce an equation.

e.g. resolving in a particular direction, taking moments about a point, applying a suvat equation, applying the conservation of momentum principle etc.

The following criteria are usually applied to the equation.

To earn the M mark, the equation

(i) should have the correct number of terms

(ii) be dimensionally correct i.e. all the terms need to be dimensionally correct

e.g. in a moments equation, every term must be a 'force x distance' term or 'mass x distance', if we allow them to cancel 'g' s.

For a resolution, all terms that need to be resolved (multiplied by sin or cos) must be resolved to earn the M mark.

M marks are sometimes dependent (DM) on previous M marks having been earned. e.g. when two simultaneous equations have been set up by, for example, resolving in two directions and there is then an M mark for solving the equations to find a particular quantity – this M mark is often dependent on the two previous M marks having been earned.

'A' marks

These are dependent accuracy (or sometimes answer) marks and can only be awarded if the previous M mark has been earned. e.g. M0 A1 is impossible.

'B' marks

These are independent accuracy marks where there is no method (e.g. often given for a comment or for a graph).

A few of the A and B marks may be f.t. – follow through – marks.

3. General Abbreviations

These are some of the traditional marking abbreviations that will appear in the mark schemes.

- bod benefit of doubt
- ft follow through
- the symbol $\sqrt{}$ will be used for correct ft
- cao correct answer only
- cso correct solution only. There must be no errors in this part of the question to obtain this mark
- isw ignore subsequent working
- awrt answers which round to
- SC special case
- oe or equivalent (and appropriate)
- dep dependent
- indep independent
- dp decimal places
- sf significant figures
- ***** The answer is printed on the paper
- _ _ The second mark is dependent on gaining the first mark
- 4. All A marks are 'correct answer only' (cao), unless shown, for example as A1 ft to indicate that previous wrong working is to be followed through. After a misread however, the subsequent A marks are treated as A ft, but manifestly absurd answers should never be awarded A marks.
- 5. For misreading which does not alter the character of a question or materially simplify it, deduct two from any A or B marks gained, in that part of the question affected.
- 6. If a candidate makes more than one attempt at any question:
 - If all but one attempt is crossed out, mark the attempt which is NOT crossed out.
 - If either all attempts are crossed out or none are crossed out, mark all the attempts and score the highest single attempt.
- 7. Ignore wrong working or incorrect statements following a correct answer.

General Principles for Mechanics Marking

(But note that specific mark schemes may sometimes override these general priniciples)

- Rules for M marks: correct no. of terms; dimensionally correct; all terms that need resolving (i.e. multiplied by cos or sin) are resolved.
- Omission or extra g in a resolution is an accuracy error not method error.
- Omission of mass from a resolution is a method error.
- Omission of a length from a moments equation is a method error.
- Omission of units or incorrect units is not (usually) counted as an accuracy error.
- DM indicates a dependent method mark i.e. one that can only be awarded if a previous specified method mark has been awarded.
- Any numerical answer which comes from use of g = 9.8 should be given to 2 or 3 SF
- Use of g = 9.81 should be penalised once per (complete) question.
 N.B. Over-accuracy or under-accuracy of correct answers should only be penalized once per complete question. However, premature approximation should be penalised every time it occurs.
- Marks must be entered in the same order as they appear on the mark scheme.
- In all cases, if the candidate clearly labels their working under a particular part of a question i.e. (a) or (b) or (c),.....then that working can only score marks for that part of the question.
- Accept column vectors in all cases.
- Misreads if a misread does not alter the character of a question or materially simplify it, deduct two from any A or B marks gained, bearing in mind that after a misread, the subsequent A marks affected are treated as A ft
- Mechanics Abbreviations
 - M(A) Taking moments about A
 - N2L Newton's Second Law (Equation of Motion)
 - NEL Newton's Experimental Law (Newton's Law of Impact
 - HL Hooke's Law
 - SHM Simple harmonic motion
 - PCLM Principle of conversation of linear momentum
 - RHS, LHS Right hand side, left hand side

Question	Scheme	Marks
Number		
1 (a)	$\pi \int_0^1 (1+\sqrt{x})^2 \mathrm{d}x$	M1
	$=\pi \left[x + \frac{4}{3}x^{\frac{3}{2}} + \frac{1}{2}x^{2} \right]_{0}^{1}$	A1
	$=\frac{17\pi}{6}$ m ³ * including units	A1*
		(3)
(b)	$\pi \int_0^1 x (1 + \sqrt{x})^2 \mathrm{d}x$	M1
	$=\pi \left[\frac{1}{2}x^{2} + \frac{4}{5}x^{\frac{5}{2}} + \frac{1}{3}x^{3}\right]_{0}^{1}$	A1
	$=\frac{49\pi}{30}$	A1
	<u>49</u> π	
	$\overline{x} = \frac{30}{\frac{17\pi}{6}}$	dM1
	$\frac{17\pi}{6} = \frac{49}{85} \text{m}^* \text{ including units}$	A1 *
		(5)
	Notes	(8)
	NB: Penalise missing units maximum of once per question.	
(a)		
M1	Use of $\pi \int_{0}^{1} (1 + \sqrt{x})^2 dx$. Limits not needed. π is required.	
A1	Correct integration – limits not needed	
A1*	Correct given answer correctly obtained. Must include units. Limits must b substitution is not required). Accept $\frac{17}{6}\pi$ m ³	e seen (sight of
(b)		
M1	Use of $\pi \int_0^1 x(1+\sqrt{x})^2 dx$. Limits not needed (π 's will cancel so it may not	be seen)
A1	Correct integration – limits not needed	
A1	Correct unsimplified with or without π (may see $\frac{1}{2} + \frac{4}{5} + \frac{1}{3} = 0$)	
dM1	Correct expression with their numerator (consistent π - seen in neither or b	poth)
A1*	Correct given answer correctly obtained. Must include units.	

Question Number	Scheme	Ma	rks
2.	$F\cos\alpha = mg$	MI	A1
	$F\sin\alpha = T$	M1	A1
	$T = \frac{2mgx}{l}$ or $T = \frac{2mg(AB-l)}{l}$	M1	<u> </u>
	$\frac{3}{4}mg = \frac{2mgx}{l}$	dM1	
	$AB = \frac{11l}{8}$	A1	
			(6)
	Notes		
M1	M1 Resolve vertically or horizontally, correct no. of terms, condone sign errors and sin/cos confusion (or use trig on a right-angled triangle of forces)		
A1	Correct vertical equation		
A1	Correct horizontal equation (A2 for $T = mg \tan \alpha$ from triangle of forces)		
M1	Hooke's Law. Must clearly be an extension and not <i>AB</i> . Since <i>x</i> is not defined in the question, other extensions may be used including $(AB - l)$ or <i>xl</i> where <i>x</i> is found to be the constant $\frac{3}{8}$.		•
dM1	Substitute trig (not necessarily correctly) to produce an equation in ' x ' (and l) only, dependent on previous M's and on having two equations.		
A1	Cao Accept 1.375 <i>l</i> , 1.4 <i>l</i> , 1.38 <i>l</i>		

Question Number	Scheme	Marks
3 (a)	Slant height, $l = \sqrt{\left(\frac{7a}{4}\right)^2 + (6a)^2} \ (=\frac{25a}{4})$	M1
	MassesSquare $16a^2$	B1 square
	Circle $\pi \left(\frac{7a}{4}\right)^2$	B1 circle
	Conical shell $\pi \times \frac{7a}{4} \times \frac{25a}{4}$	B1ft (shell
	Total $\left[16a^2 - \pi \left(\frac{7a}{4}\right)^2 + \pi \times \frac{7a}{4} \times \frac{25a}{4}\right]$	and total)
	DistancesSquareCircleConical shellTotal00 $2a$: \bar{x}	B1
	$\pi \times \frac{7a}{4} \times \frac{25a}{4} \times 2a = \left[16a^2 - \pi \left(\frac{7a}{4}\right)^2 + \pi \times \frac{7a}{4} \times \frac{25a}{4}\right] \overline{x}$	M1 A1
	$\overline{x} = \frac{175\pi a}{(63\pi + 128)} *$	A1*
		(8)
3 (b)	$\tan \alpha = \frac{2a}{\left(\frac{175\pi a}{(63\pi + 128)}\right)}$	M1
	$\tan \alpha = \frac{126\pi + 256}{175\pi}$ (or $\frac{2(63\pi + 128)}{175\pi}$)	A1
		(2)
	NT-4	(10)
(a)	Notes	
<u>(a)</u> M1	Use of Pythagoras (unsimplified). May be seen on the diagram.	
B1	Mass/area of square	
B1	Mass/area of circle	
B1 ft	Mass/area of conical shell and total. A common error is to use 6 <i>a</i> as slant height, only ft on their calculated slant height. May derive conical shell formula from area of a sector.	
B1	All distances correct	
M1	Dimensionally correct moments equation. Must have correct number of terms including an attempt to subtract the circle. Condone a slip with an 'a' in one term.	
A1	Correct equation (no ft)Given answer correctly obtained. Condone missing brackets from denominator and terms	
A1*	reversed.	
(b)		
M1	Allow reciprocal. Must use $2a$ and given \overline{x} .	
A1	Cao Exact fraction required.	

Question Number	Scheme	Marks
4(a)	$a = v \frac{\mathrm{d}v}{\mathrm{d}x}$	M1
	$=\frac{3}{2}(2x+1)^{\frac{1}{2}} \times 2 \times (2x+1)^{\frac{3}{2}} = 3(2x+1)^{2}$	A1
	$3(2x+1)^2=243$	M1
	x = 4	A1
		(4)
4(b)	$(2x+1)^{\frac{3}{2}} = \frac{dx}{dt} \qquad OR \qquad a = 3v^{\frac{4}{3}} = \frac{dv}{dt}$ $\int dt = \int (2x+1)^{\frac{3}{2}} dx \qquad \int 3dt = \int v^{-\frac{4}{3}} dv$ $t = -(2x+1)^{\frac{1}{2}} (+C) \qquad 3t + (C) = -3v^{-\frac{1}{3}}$	M1 A1
	$\int dt = \int (2x+1)^{\frac{3}{2}} dx \qquad \int 3dt = \int v^{-\frac{4}{3}} dv$ $t = -(2x+1)^{\frac{1}{2}} (+C) \qquad 3t + (C) = -3v^{-\frac{1}{3}}$	M1
	$t = -(2x+1)^{\frac{1}{2}}(+C) \qquad \qquad 3t + (C) = -3v^{\frac{1}{3}}$	A1
	$t = 0, x = 0 \Longrightarrow C = 1$ and obtain an equation in v and t only. $t = 0, x = 0 \Longrightarrow v = 1 \Longrightarrow C = -3$	M1
	$v = \frac{1}{\left(1 - t\right)^3}$	A1
		(6)
		(10)
	Notes	
(a)	$1 \qquad 1 \qquad 1 \qquad 1 \qquad $	
M1	Use of $a = v \frac{dv}{dx}$ or $a = \frac{d}{dx} \left(\frac{1}{2}v^2\right)$. Evidence of differentiation, power decreases	sing by 1.
	Should see a product of terms to imply 'use of'.	
A1 M1	Correct differentiation Indexed on the product from differentiation and put $a = 242$ then eally	for a
M1 A1	Independent. Use their result from differentiation and put $a = 243$ then solve Cao If -5 is seen then it must be rejected or 4 must be clearly identified.	10f X
(b)	Cao II -5 is seen then it must be rejected of 7 must be clearly identified.	
M1	Use of $v = \frac{dx}{dt}$ to obtain DE in x and t OR Use of $a = \frac{dv}{dt}$ to obtain I	DE in <i>v</i> and <i>t</i>
A1	Correct equation	
M1	Separate and integrate (evidence of integration, power increasing by 1)	
A1	Correct integration, condone missing C	
M1	Use $t = 0$, $x = 0$ to obtain a value of C and obtain an equation in v and t only.	
A1	Cao Accept $v = (1-t)^{-3}$ or $v = \frac{-1}{(t-1)^3}$ or $v = -(t-1)^{-3}$	
	Note: No marks in (b) for use of $a = 243$	

Question Number	Scheme	Marks
5(a)	Use of cosine rule on triangle <i>APB</i> OR trig. on 'half' of the triangle <i>APB</i> to find one relevant angle.	M1
	Given answers correctly obtained.*	A1* (2)
5(b)	$T_A \cos 30^\circ + T_B \cos 60^\circ = mg$	M1 A1
	$T_A \sin 30^\circ + T_B \sin 60^\circ = mr\omega^2$	M1A1A1
	$r = a \sin 60^{\circ} \text{ (or } r = a\sqrt{3}\cos 30 \text{ or } r = a\frac{\sqrt{3}}{2}\text{)}$	B1
	Solve for T_A	dM1
	$T_A = \frac{1}{2}m\sqrt{3}(2g - a\omega^2) *$	A1*
5(a)		(8) M1
5(c)	Attempt to obtain one inequality on ω^2 Correct inequality	Al
	Attempt to obtain another inequality on ω^2 and use both to obtain answer	M1
	$\frac{2g}{3a} < \omega^2 < \frac{2g}{a} *$	A1 *
		(4)
		(14)
	Notes	(14)
(a) M1		(14)
(a) M1	Either complete method to obtain one relevant angle.	
		leading to both
M1	Either complete method to obtain one relevant angle. Correct GIVEN angles correctly obtained. Sufficient annotation/justification given answers eg Stating $\angle OBP = 2 \times \angle OAP$ alone is not sufficient – addition or justification is required. Use of triangles to verify is acceptable.	leading to both
M1 A1* (b) M1	Either complete method to obtain one relevant angle.Correct GIVEN angles correctly obtained. Sufficient annotation/justificationgiven answers eg Stating $\angle OBP = 2 \times \angle OAP$ alone is not sufficient – additionor justification is required. Use of triangles to verify is acceptable.Resolve vertically, dimensionally correct equation with correct no. of terms,errors and sin/cos confusion.	leading to both
M1 A1* (b)	Either complete method to obtain one relevant angle.Correct GIVEN angles correctly obtained. Sufficient annotation/justificationgiven answers eg Stating $\angle OBP = 2 \times \angle OAP$ alone is not sufficient – additionor justification is required. Use of triangles to verify is acceptable.Resolve vertically, dimensionally correct equation with correct no. of terms, errors and sin/cos confusion.Correct equation	leading to both onal annotation condone sign
M1 A1* (b) M1	Either complete method to obtain one relevant angle.Correct GIVEN angles correctly obtained. Sufficient annotation/justificationgiven answers eg Stating $\angle OBP = 2 \times \angle OAP$ alone is not sufficient – additionor justification is required. Use of triangles to verify is acceptable.Resolve vertically, dimensionally correct equation with correct no. of terms,errors and sin/cos confusion.Correct equationEquation of motion horizontally: dimensionally correct equation with correct equation with correct condone sign errors and sin/cos confusion.	leading to both onal annotation condone sign t no. of terms,
M1 A1* (b) M1 A1 M1 A1	Either complete method to obtain one relevant angle. Correct GIVEN angles correctly obtained. Sufficient annotation/justification given answers eg Stating $\angle OBP = 2 \times \angle OAP$ alone is not sufficient – addition or justification is required. Use of triangles to verify is acceptable. Resolve vertically, dimensionally correct equation with correct no. of terms, errors and sin/cos confusion. Correct equation Equation of motion horizontally: dimensionally correct equation with correct condone sign errors and sin/cos confusion. Correct equation, with at most one error. If $r\omega^2$ is never seen, this is an A error	leading to both onal annotation condone sign t no. of terms,
M1 A1* (b) M1 A1 M1 A1 A1 A1	Either complete method to obtain one relevant angle. Correct GIVEN angles correctly obtained. Sufficient annotation/justification given answers eg Stating $\angle OBP = 2 \times \angle OAP$ alone is not sufficient – addition or justification is required. Use of triangles to verify is acceptable. Resolve vertically, dimensionally correct equation with correct no. of terms, errors and sin/cos confusion. Correct equation Equation of motion horizontally: dimensionally correct equation with correct condone sign errors and sin/cos confusion. Correct equation, with at most one error. If $r\omega^2$ is never seen, this is an A err Correct equation	leading to both onal annotation condone sign t no. of terms,
M1 A1* (b) M1 A1 M1 A1 A1 A1 B1	Either complete method to obtain one relevant angle. Correct GIVEN angles correctly obtained. Sufficient annotation/justification given answers eg Stating $\angle OBP = 2 \times \angle OAP$ alone is not sufficient – addition or justification is required. Use of triangles to verify is acceptable. Resolve vertically, dimensionally correct equation with correct no. of terms, errors and sin/cos confusion. Correct equation Equation of motion horizontally: dimensionally correct equation with correct condone sign errors and sin/cos confusion. Correct equation, with at most one error. If $r\omega^2$ is never seen, this is an A err Correct equation Cao If this is seen in (a) it must be used in (b) for this mark.	leading to both onal annotation condone sign t no. of terms,
M1 A1* (b) M1 A1 A1 A1 A1 B1 dM1	Either complete method to obtain one relevant angle. Correct GIVEN angles correctly obtained. Sufficient annotation/justification given answers eg Stating $\angle OBP = 2 \times \angle OAP$ alone is not sufficient – addition or justification is required. Use of triangles to verify is acceptable. Resolve vertically, dimensionally correct equation with correct no. of terms, errors and sin/cos confusion. Correct equation Equation of motion horizontally: dimensionally correct equation with correct condone sign errors and sin/cos confusion. Correct equation, with at most one error. If $r\omega^2$ is never seen, this is an A err Correct equation Cao If this is seen in (a) it must be used in (b) for this mark. Solve for T_A in terms of <i>m</i> , <i>a</i> , <i>g</i> and ω	leading to both onal annotation condone sign t no. of terms,
M1 A1* (b) M1 A1 M1 A1 A1 B1 dM1 A1*	Either complete method to obtain one relevant angle. Correct GIVEN angles correctly obtained. Sufficient annotation/justification given answers eg Stating $\angle OBP = 2 \times \angle OAP$ alone is not sufficient – addition or justification is required. Use of triangles to verify is acceptable. Resolve vertically, dimensionally correct equation with correct no. of terms, errors and sin/cos confusion. Correct equation Equation of motion horizontally: dimensionally correct equation with correct condone sign errors and sin/cos confusion. Correct equation, with at most one error. If $r\omega^2$ is never seen, this is an A err Correct equation Cao If this is seen in (a) it must be used in (b) for this mark.	leading to both onal annotation condone sign t no. of terms,
M1 A1* (b) M1 A1 A1 A1 A1 B1 dM1	Either complete method to obtain one relevant angle. Correct GIVEN angles correctly obtained. Sufficient annotation/justification given answers eg Stating $\angle OBP = 2 \times \angle OAP$ alone is not sufficient – addition or justification is required. Use of triangles to verify is acceptable. Resolve vertically, dimensionally correct equation with correct no. of terms, errors and sin/cos confusion. Correct equation Equation of motion horizontally: dimensionally correct equation with correct condone sign errors and sin/cos confusion. Correct equation, with at most one error. If $r\omega^2$ is never seen, this is an A err Correct equation Cao If this is seen in (a) it must be used in (b) for this mark. Solve for T_A in terms of <i>m</i> , <i>a</i> , <i>g</i> and ω Given answer correctly obtained. Must see exactly.	leading to both onal annotation condone sign t no. of terms, or.
M1 A1* (b) M1 A1 M1 A1 A1 B1 dM1 A1*	Either complete method to obtain one relevant angle. Correct GIVEN angles correctly obtained. Sufficient annotation/justification given answers eg Stating $\angle OBP = 2 \times \angle OAP$ alone is not sufficient – addition or justification is required. Use of triangles to verify is acceptable. Resolve vertically, dimensionally correct equation with correct no. of terms, errors and sin/cos confusion. Correct equation Equation of motion horizontally: dimensionally correct equation with correct condone sign errors and sin/cos confusion. Correct equation, with at most one error. If $r\omega^2$ is never seen, this is an A err Correct equation Cao If this is seen in (a) it must be used in (b) for this mark. Solve for T_A in terms of m , a , g and ω Given answer correctly obtained. Must see exactly. Correct use of either $T_A > 0$ or their $T_B > 0$ oe to obtain one inequality on ω^2	leading to both onal annotation condone sign t no. of terms, or.
M1 A1* (b) M1 A1 A1 A1 B1 dM1 A1* (c)	Either complete method to obtain one relevant angle. Correct GIVEN angles correctly obtained. Sufficient annotation/justification given answers eg Stating $\angle OBP = 2 \times \angle OAP$ alone is not sufficient – addition or justification is required. Use of triangles to verify is acceptable. Resolve vertically, dimensionally correct equation with correct no. of terms, errors and sin/cos confusion. Correct equation Equation of motion horizontally: dimensionally correct equation with correct condone sign errors and sin/cos confusion. Correct equation, with at most one error. If $r\omega^2$ is never seen, this is an A err Correct equation Cao If this is seen in (a) it must be used in (b) for this mark. Solve for T_A in terms of <i>m</i> , <i>a</i> , <i>g</i> and ω Given answer correctly obtained. Must see exactly.	leading to both onal annotation condone sign t no. of terms, or.
M1 A1* (b) M1 A1 A1 A1 B1 dM1 A1* (c) M1	Either complete method to obtain one relevant angle. Correct GIVEN angles correctly obtained. Sufficient annotation/justification given answers eg Stating $\angle OBP = 2 \times \angle OAP$ alone is not sufficient – addition or justification is required. Use of triangles to verify is acceptable. Resolve vertically, dimensionally correct equation with correct no. of terms, errors and sin/cos confusion. Correct equation Equation of motion horizontally: dimensionally correct equation with correct condone sign errors and sin/cos confusion. Correct equation, with at most one error. If $r\omega^2$ is never seen, this is an A err Correct equation Cao If this is seen in (a) it must be used in (b) for this mark. Solve for T_A in terms of m , a , g and ω Given answer correctly obtained. Must see exactly. Correct use of either $T_A > 0$ or their $T_B > 0$ oe to obtain one inequality on ω^2 expression for either Tension > 0.	leading to both onal annotation condone sign t no. of terms, or.
M1 A1* (b) M1 A1 A1 A1 B1 dM1 A1* (c) M1	Either complete method to obtain one relevant angle. Correct GIVEN angles correctly obtained. Sufficient annotation/justification given answers eg Stating $\angle OBP = 2 \times \angle OAP$ alone is not sufficient – addition or justification is required. Use of triangles to verify is acceptable. Resolve vertically, dimensionally correct equation with correct no. of terms, errors and sin/cos confusion. Correct equation Equation of motion horizontally: dimensionally correct equation with correct condone sign errors and sin/cos confusion. Correct equation, with at most one error. If $r\omega^2$ is never seen, this is an A err Correct equation Cao If this is seen in (a) it must be used in (b) for this mark. Solve for T_A in terms of m , a , g and ω Given answer correctly obtained. Must see exactly. Correct use of either $T_A > 0$ or their $T_B > 0$ oe to obtain one inequality on ω^2 expression for either Tension > 0. Correct inequality	leading to both onal annotation condone sign t no. of terms, or.

Question Number	Scheme	Marks
6(a)	$\frac{1}{2}mv^2 - mgl$ or $mgl - \frac{1}{2}mv^2$ seen or implied	B1
	Use of EPE	M1
	$\frac{mg}{2l}l^2$	A1
	$\frac{mg}{2l}(l\sqrt{2}-l)^2$	A1
	$\frac{1}{2}mv^2 + \frac{mg}{2l}(l\sqrt{2}-l)^2 = mgl + \frac{mg}{2l}l^2$ Solve for v^2	M1
	Solve for v^2	dM1
	$v^2 = 2gl\sqrt{2} *$	A1*
		(7)
(b)	$T = \frac{mg(l\sqrt{2}-l)}{l} = mg(\sqrt{2}-1)$ $\pm N + T\cos 45^{\circ} = \frac{mv^{2}}{l}$ $\pm N + mg(\sqrt{2}-1) \times \frac{\sqrt{2}}{2} = \frac{m}{l} \times 2gl\sqrt{2}$	M1 A1
	$\pm N + T\cos 45^\circ = \frac{mv^2}{l}$	M1A1A1
	$\pm N + mg(\sqrt{2} - 1) \times \frac{\sqrt{2}}{2} = \frac{m}{l} \times 2gl\sqrt{2}$	dM1
	$\mathbf{*}$ $N = \frac{1}{2}mg(5\sqrt{2}-2)$	A1*
		(7)
	Notas	(14)
(a)	Notes	
<u>(a)</u> B1	Difference between KE and GPE, seen either way round.	
M1	Use of EPE formula at top or at <i>B</i>	
A1	Correct EPE at top	
A1	Correct EPE at B	
M1	Use of conservation of energy, with 1 GPE, 1 KE and 2 EPE terms, condone sign errors	
<u>dM1</u>	Solve for v^2 , dependent on previous M	
A1*	Exact given answer correctly obtained	
(b) M1	Use of Hooke's Law at B – this may appear in an attempted equation of motion	
A1	Correct unsimplified tension at <i>B</i>	
M1	Equation of motion at <i>B</i> horizontally with correct terms, condone sign error	S
A1	Correct equation with at most one error	
A1	Correct equation	
dM1	Sub for T and v^2 . Dependent on both previous M marks	
A1*	Given answer correctly obtained (exactly). If $N = -\frac{1}{2}mg(5\sqrt{2}-2)$ then clearly	
	is required to reach the given answer eg use of 'magnitude' or modulus sign	IS.

Question Number	Scheme	Marks
7(a)	$T_A - T_B = m\ddot{x}$	M1
	$\frac{2mg}{l}\left(\frac{2l}{3}-x\right)-\frac{mg}{l}\left(\frac{4l}{3}+x\right)=m\ddot{x} \text{or} \frac{mg}{l}\left(\frac{4l}{3}-x\right)-\frac{2mg}{l}\left(\frac{2l}{3}+x\right)=m\ddot{x}.$	dM1A1
	$-\frac{3g}{l}x = \ddot{x}$, so SHM	A1
	$T = \frac{2\pi}{\sqrt{\frac{3g}{l}}} = 2\pi\sqrt{\frac{l}{3g}} *$	M1 A1*
		(6)
7(b)	$\frac{1}{2}l \times \sqrt{\frac{3g}{l}}$ or $\frac{1}{2}\sqrt{3gl}$ or $\sqrt{\frac{3gl}{4}}$ oe	B1
		(1)
7(c)	$\frac{3g}{2}$ or 1.5g	B1
		(1)
7(d)	$x = a\cos\omega t \Longrightarrow v = -a\omega\sin\omega t$	M1
	$-\frac{3}{4}\sqrt{gl} = -a\omega\sin\omega t \text{to find } t$	M1A1
	Solve for <i>t</i>	M1
	$t = \frac{\pi}{3} \sqrt{\frac{l}{3g}} \text{oe}$	A1
		(5)
		(13)
(a)	Notes	
M1	Equation of motion in a <i>general</i> position, allow <i>a</i> for acceleration, correct no. condone sign errors.	of terms,
dM1	Use Hooke's Law to sub for the two tensions, allow <i>a</i> for acceleration. Extensions must be different and of the form $(d \pm x)$ where <i>d</i> is a multiple of <i>l</i> .	
A1	Correct unsimplified equation, allow <i>a</i> for acceleration.	
A1	Correct equation using \ddot{x} for acceleration.	
M1	Use of $\frac{2\pi}{\omega}$ Their ω from their equation of motion, which must be in terms of x.	
A1*cso	Given answer correctly obtained – this includes proof of SHM with conclusion and correct expression for the period.	
(b)		
B1	Cao Speed at <i>O</i> so must be positive. Unsimplified, ignore errors from subsequésimplifying' of surds.	uent
(c)		
B1	Cao Max acceleration so must be positive.	

(d)	
Main	
Main M1	Use of $x = a \cos \omega t$ to obtain $v = -a\omega \sin \omega t$ Substitution for a and ω is not required.
M1	Use $v = -a\omega\sin\omega t$ with $a = \frac{l}{2}$ and $\omega = \sqrt{\frac{3g}{l}}$ to obtain equation in t only, $-\frac{3}{4}\sqrt{gl} = -a\omega\sin\omega t$
A1	Correct equation in t only
M1	Solve to find the required time, t
A1	Cao for required time.
ALT 1	
M1	Use of $x = a \sin \omega t$ to obtain $v = a \omega \cos \omega t$ Substitution for a and ω is not required.
M1	Use $v = a\omega \cos \omega t$ with $a = \frac{l}{2}$ and $\omega = \sqrt{\frac{3g}{l}}$ to obtain equation in t only, $\frac{3}{4}\sqrt{gl} = a\omega \cos \omega t$
A1	Correct equation in t only
M1	Solve to find t and then subtract from $\frac{1}{4}$ period to find the required time. $t = \frac{\pi}{6}\sqrt{\frac{l}{3g}} \implies \text{required time} = \frac{1}{4}\left(2\pi\sqrt{\frac{l}{3g}}\right) - \frac{\pi}{6}\sqrt{\frac{l}{3g}} = \frac{\pi}{3}\sqrt{\frac{l}{3g}}$
A1	Cao for required time, $t = \frac{\pi}{3} \sqrt{\frac{l}{3g}}$ oe
ALT2	
M1	Use of $x = a \cos \omega t$ or use of $x = a \sin \omega t$. Substitution for a and ω is not required.
M1	Using $v^2 = \omega^2 (a^2 - x^2)$ with $a = \frac{l}{2}$ and $\omega = \sqrt{\frac{3g}{l}}$ to obtain equation in x only. $\left(-\frac{3}{4}\sqrt{gl}\right)^2 = \omega^2 (a^2 - x^2)$
A1	Correct equation in x only. (Solution leads onto the first M mark in (d))
M1	Solves for t and then completes the method to find the required time. $\frac{l}{4} = \frac{l}{2} \cos\left(\sqrt{\frac{3g}{l}}t\right)$ or quarter period with sin method.
A1	Cao for required time, $t = \frac{\pi}{3} \sqrt{\frac{l}{3g}}$ oe
SPECIA	L CASE where $a = \frac{1}{2}$ is clearly stated as amplitude and consistently used in (b) (c) & (d)
(b)	B1 $\frac{1}{2}\sqrt{\frac{3g}{l}}$
(c)	B1 $\frac{3g}{2l}$
(d)	Maximum M1 M1 A0 M0 A0